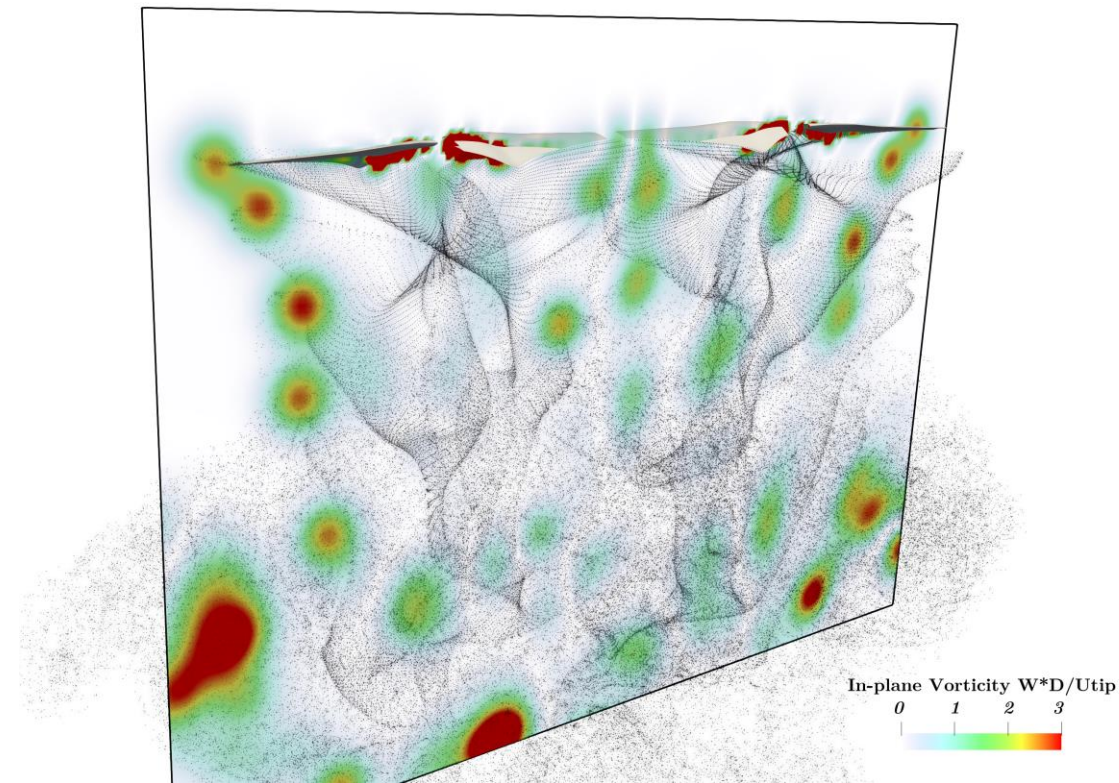


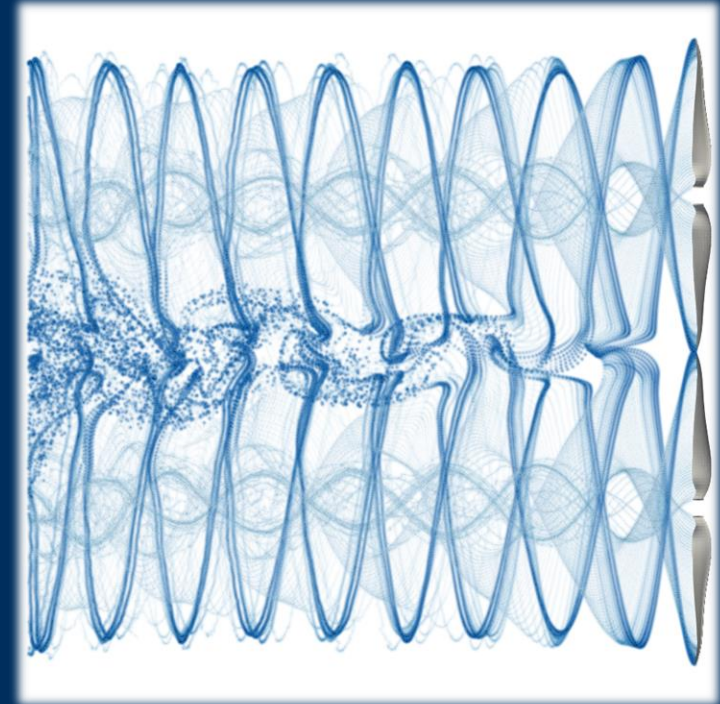
# Modeling Multirotor Aerodynamic Interactions Through the Vortex Particle Method

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# OUTLINE

- **Motivation**
- **Viscous Vortex Particle Method**
- **Propeller Model**
- **Results**
  - Individual rotor validation
  - Multirotor validation
  - Parametric study



# Motivation

- eVTOL UAM is projected to grow into a \$1.5 trillion industry.
- However, conventional analysis tools are unfit for conceptual design.



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© A<sup>3</sup> by Airbus, Vahana



© Joby Aviation



© Kitty Hawk, Flyer



© Wing

# ANALYSIS TOOLS



Momentum Theory

Free-wake Vortex Panel/Filament

RANS / LES

Viscous?	X	X	✓
Unsteady?	X	✓	✓
Wake Mixing?	X	X	✓
Fast Enough for Design?	✓	~	X

# ANALYSIS TOOLS



Momentum Theory

Free-wake Vortex Panel/Filament

Vortex Particle Method

RANS / LES

Viscous?

X

X

✓

✓

Unsteady?

X

✓

✓

✓

Wake Mixing?

X

X

✓

✓

Fast Enough for Design?

✓

~

~

X

# ANALYSIS TOOLS



## Vortex Particle Method

- Vorticity form of Navier-Stokes in Lagrangian scheme.



# ANALYSIS TOOLS



## Vortex Particle Method

- Vorticity form of Navier-Stokes in Lagrangian scheme.

$$\nabla \times \left( \frac{D\mathbf{u}}{Dt} \right) = \nabla \times \left( -\frac{1}{\rho} \nabla p + \nu \nabla^2 \mathbf{u} \right)$$
$$\Rightarrow \frac{D\boldsymbol{\omega}}{Dt} = (\boldsymbol{\omega} \cdot \nabla) \mathbf{u} + \nu \nabla^2 \boldsymbol{\omega}$$

Particle discretization

$$\boldsymbol{\omega}(\mathbf{x}) \approx \sum_p \Gamma_p \zeta_\sigma(\mathbf{x} - \mathbf{x}_p)$$

### Governing Equations

$$\bullet \frac{d\mathbf{x}_p}{dt} = \mathbf{u}(\mathbf{x}_p)$$

$$\bullet \frac{d\Gamma_p}{dt} = (\Gamma_p \cdot \nabla) \mathbf{u}(\mathbf{x}_p) + \left. \frac{d\Gamma_p}{dt} \right|_{\text{visc}}$$

# ANALYSIS TOOLS

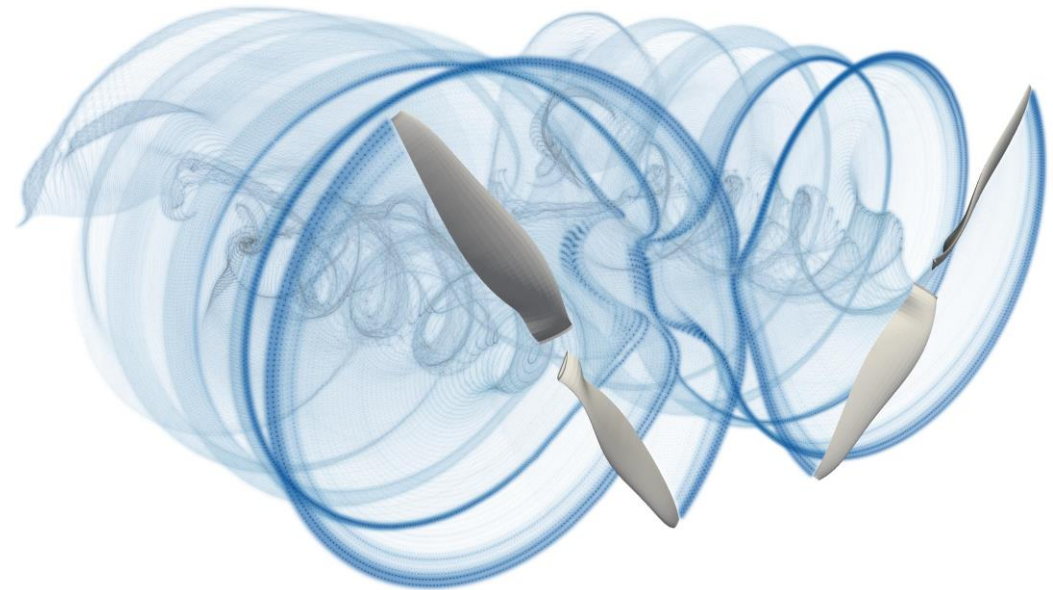
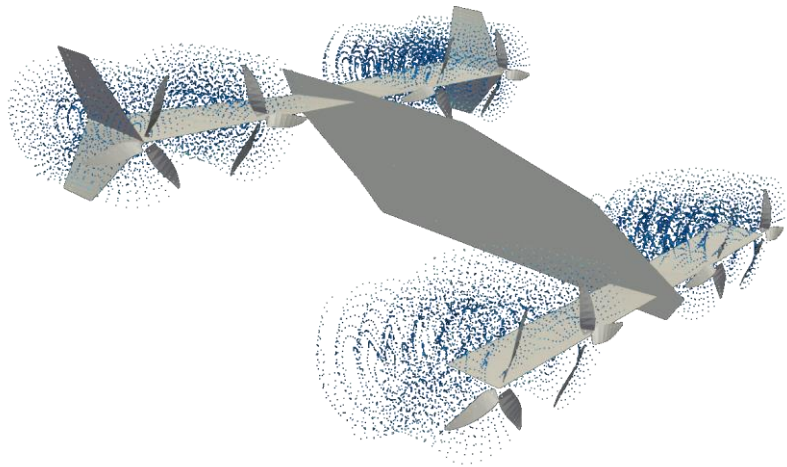


## Vortex Particle Method

- Vorticity form of Navier-Stokes in Lagrangian scheme.
- Captures viscous diffusion, vortex mixing, and decay.
- Computationally inexpensive.
- CPU and GPU parallelizable.
- Meshless.



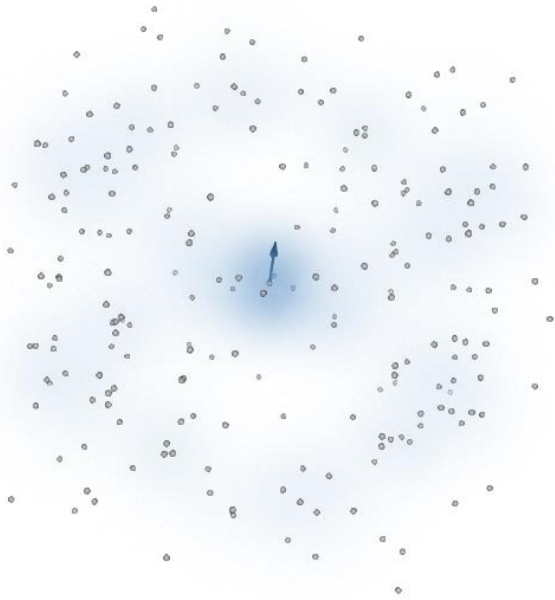
# Variable-fidelity models through VPM



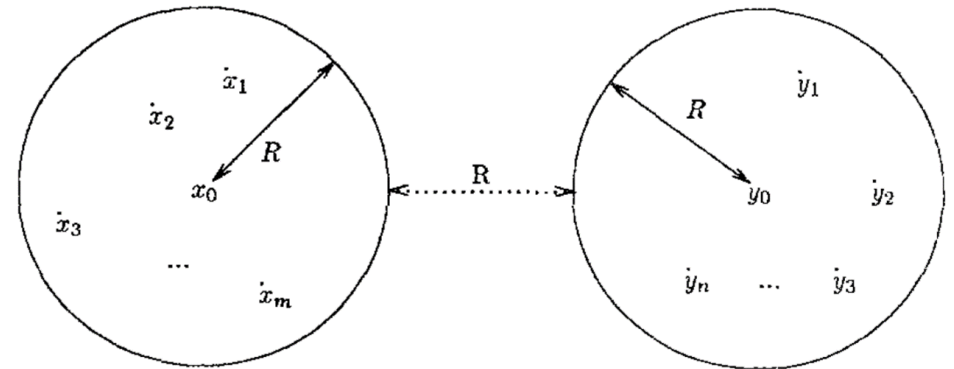
 <https://youtu.be/CP4jl7lLags>

# VPM Scaling

$N$ -body problem  $\mathcal{O}(N^2)$



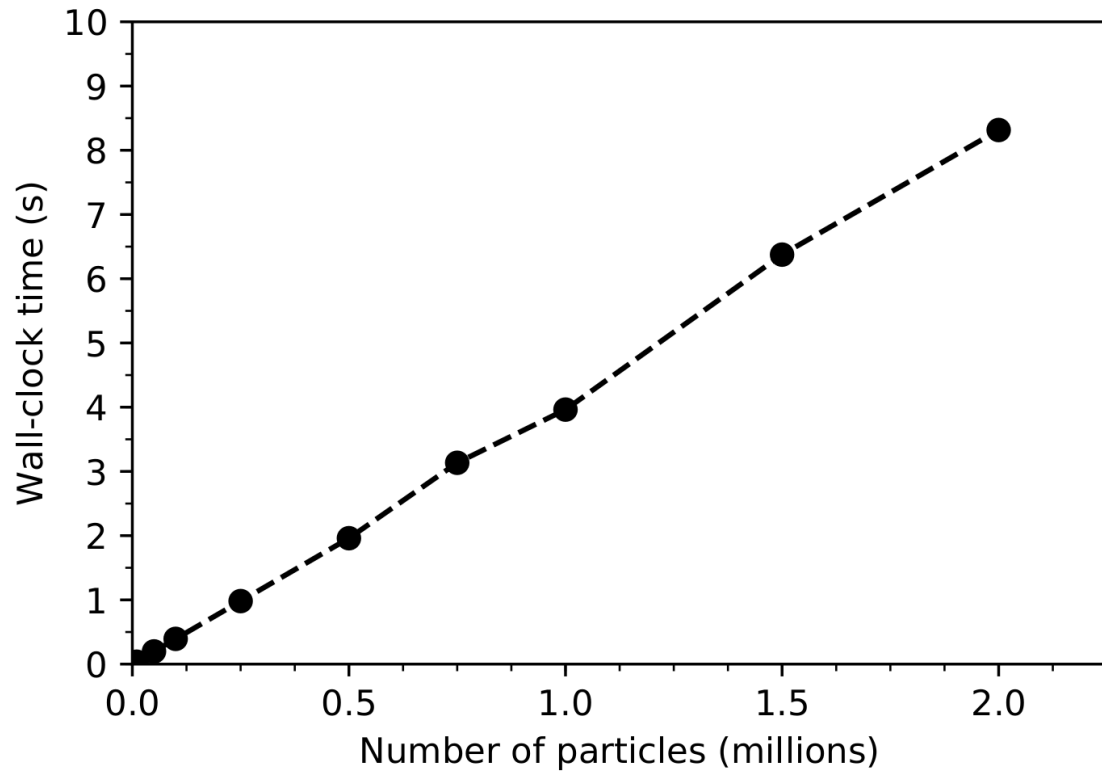
Fast multipole approximation<sup>[1,2]</sup>



[1] [www.bu.edu/exafmm](http://www.bu.edu/exafmm)

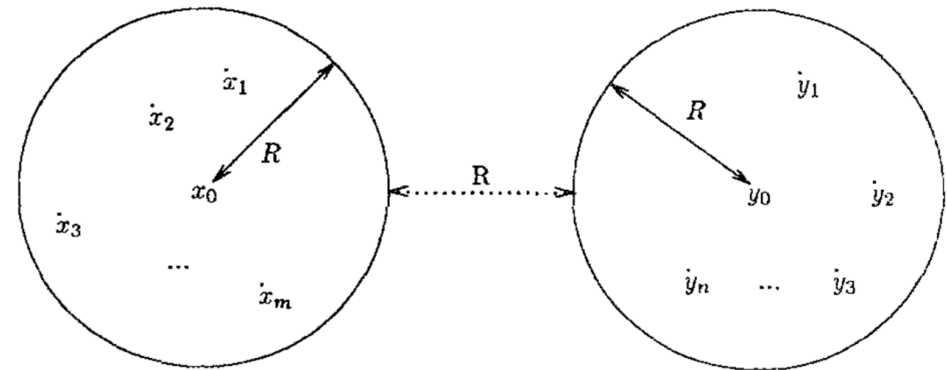
[2] Yokota, R. and Barba, L. A., 2011, "Treecode and fast multipole method for N-body simulation with CUDA."

# VPM Scaling



## Fast multipole approximation<sup>[1,2]</sup>

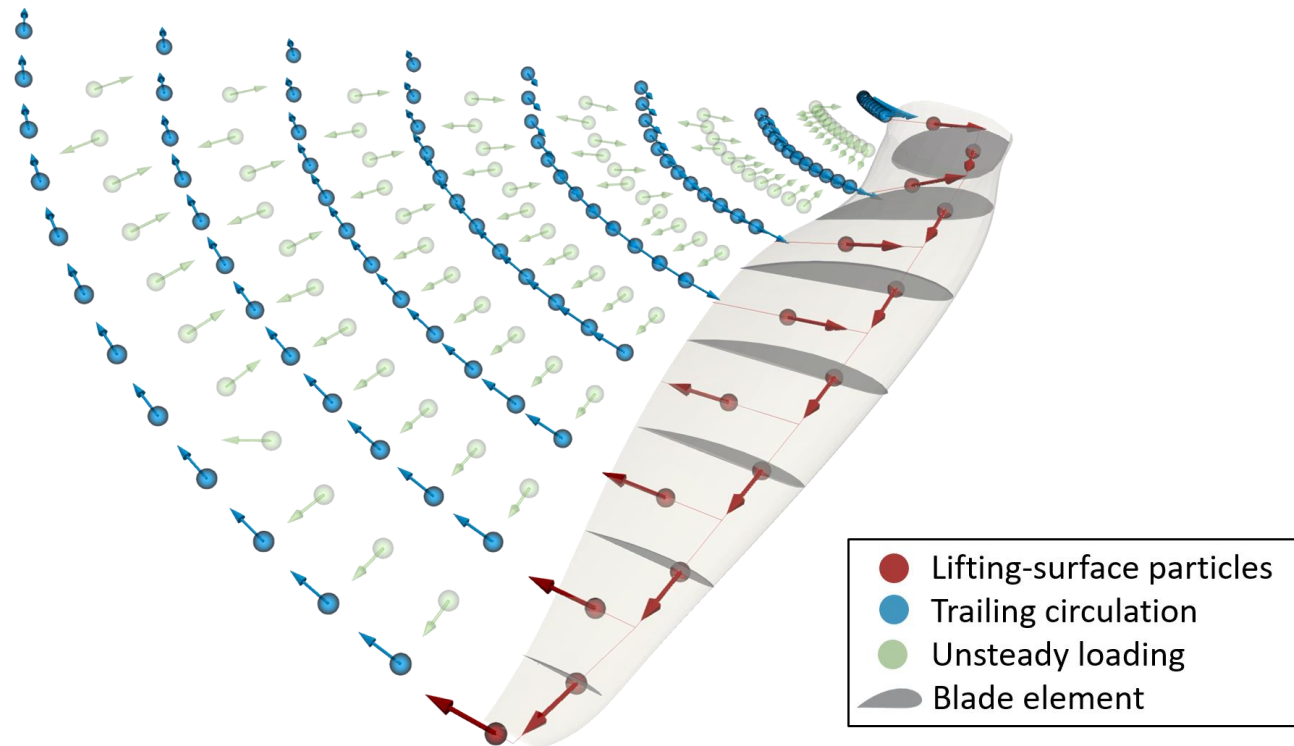
- $\mathcal{O}(N)$  scaling
- CPU and GPU scalable



[1] [www.bu.edu/exafmm](http://www.bu.edu/exafmm)

[2] Yokota, R. and Barba, L. A., 2011, "Treecode and fast multipole method for N-body simulation with CUDA."

# Propeller Model



## TEMPORAL RESOLUTION

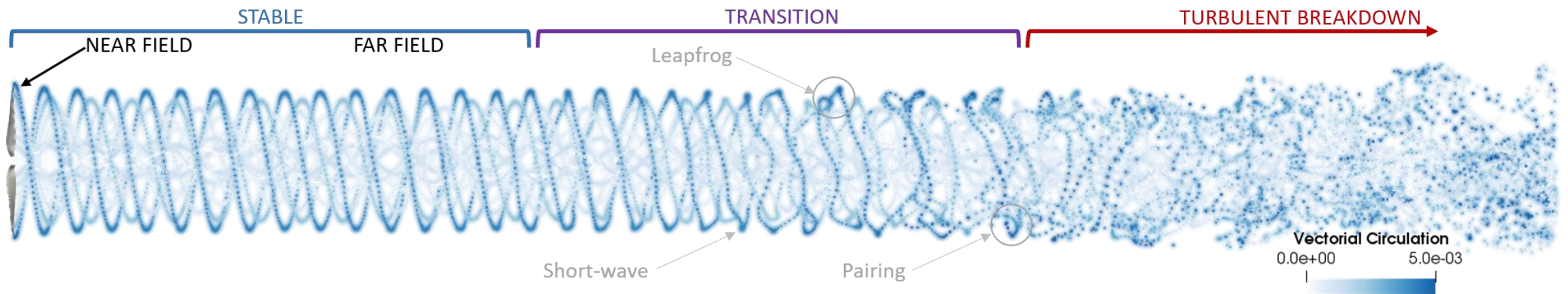
- 3<sup>rd</sup> order Runge-Kutta
- $\Delta t \rightarrow 5^\circ$  rotation

## SPATIAL RESOLUTION

- 50 elements per blade
- 2 particles shed per step
- Core overlap  $\sigma$  twice the distance between particles

- Particles are created from every source of vorticity (as colored).
- Modeling lifting surfaces through embedded particles allows linear scaling of simulations,  $\mathcal{O}(N)$ .

# Propeller Model



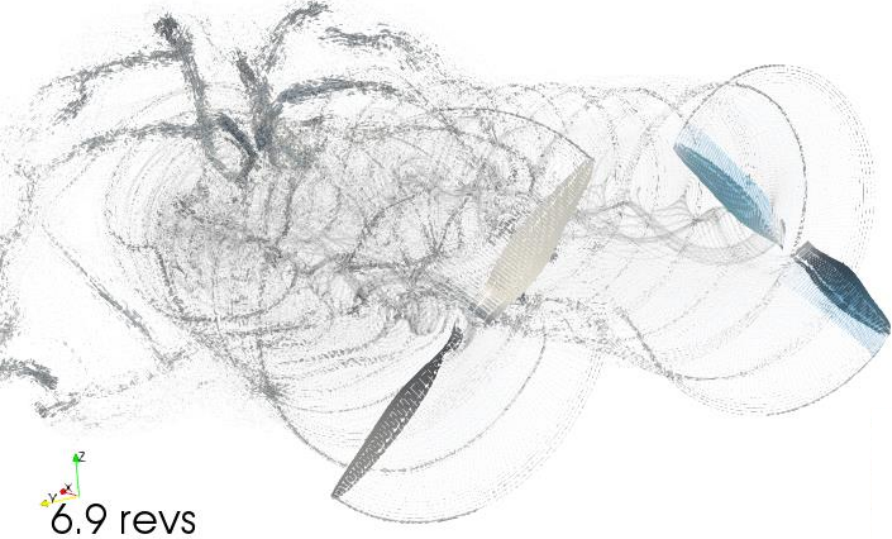
VPM captures all vortex dynamics  
from near field down to turbulent breakdown

Alvarez, E. and Ning, A., AVIATION 2018,  
**“Development of a Vortex Particle Code for the Modeling  
of Wake Interaction in Distributed Propulsion”**  
<https://scholarsarchive.byu.edu/facpub/2116/>

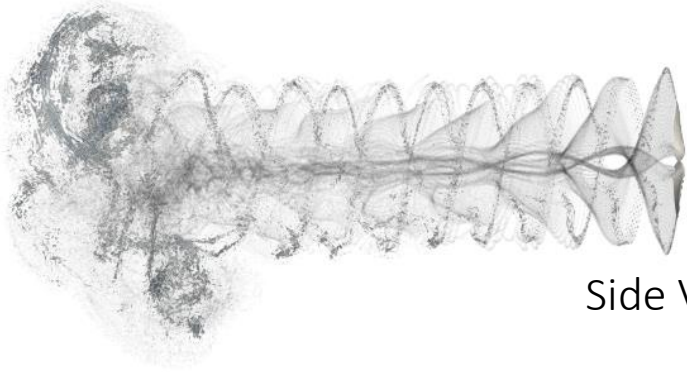
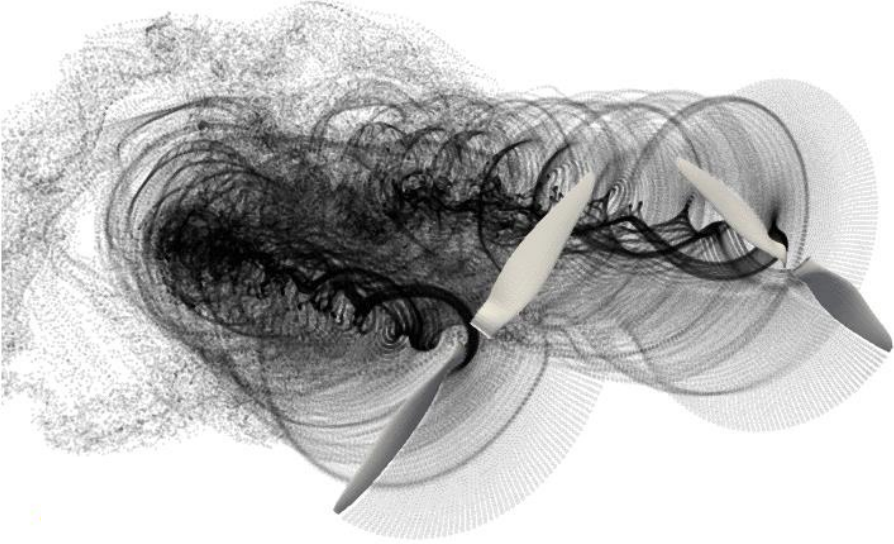


# Example Simulation

Vectorial Circulation



Particles



Side View

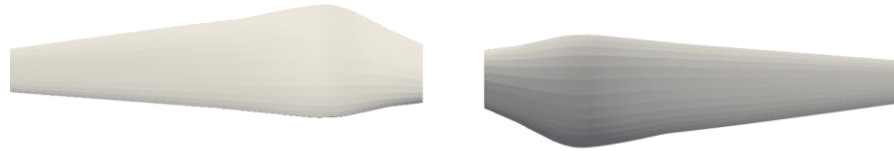


<https://youtu.be/SLpnVIBpkps>

# Test Cases

## Hover, low Reynolds

DJI Phantom II



## Forward flight, high Reynolds

APC 10x7



PARAMETER	DJI Phantom II	APC 10x7
Diameter	9.4 in (240 mm)	10 in (254 mm)
Speed	4800 RPM	9200 RPM
Tip speed	0.18 Mach	0.36 Mach
Freestream	0 m/s	0 – 27 m/s
Advance ratio	0	0 – 0.75
Chord-based Reynolds	$6.2 \times 10^4$	$1.2 \times 10^5$
Diameter-based Reynolds	$6.5 \times 10^5$	$1.5 \times 10^6$

$$Re_c = \frac{V_{0.7} \bar{c}}{\nu}$$

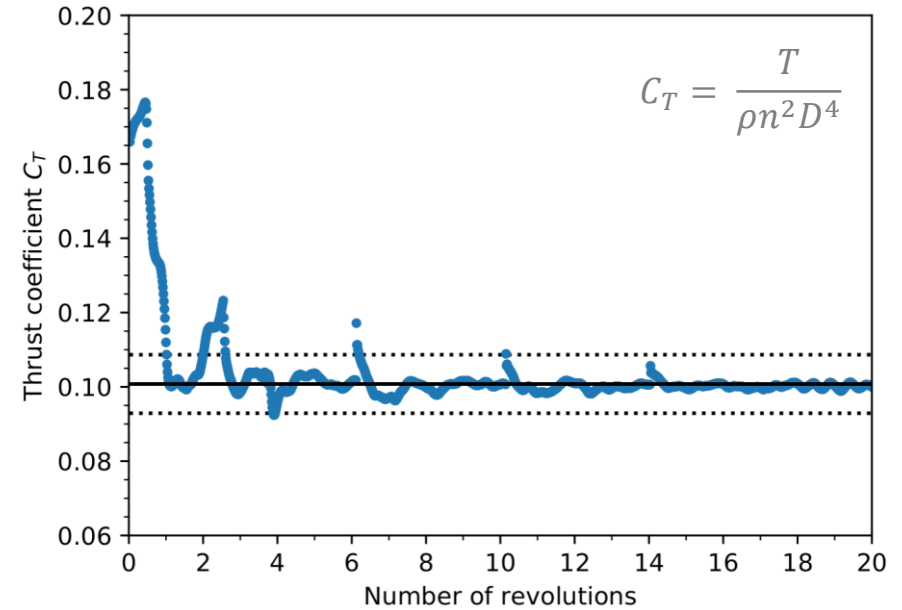
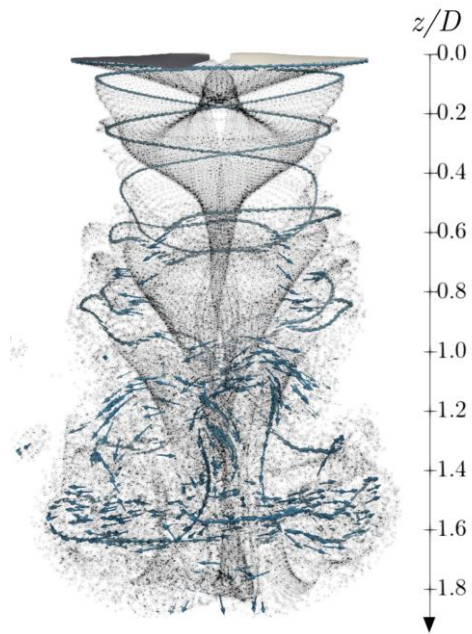
$$Re_D = \frac{V_{0.7} D}{\nu}$$



RESULTS

# INDIVIDUAL ROTOR

# Hover – Individual Rotor



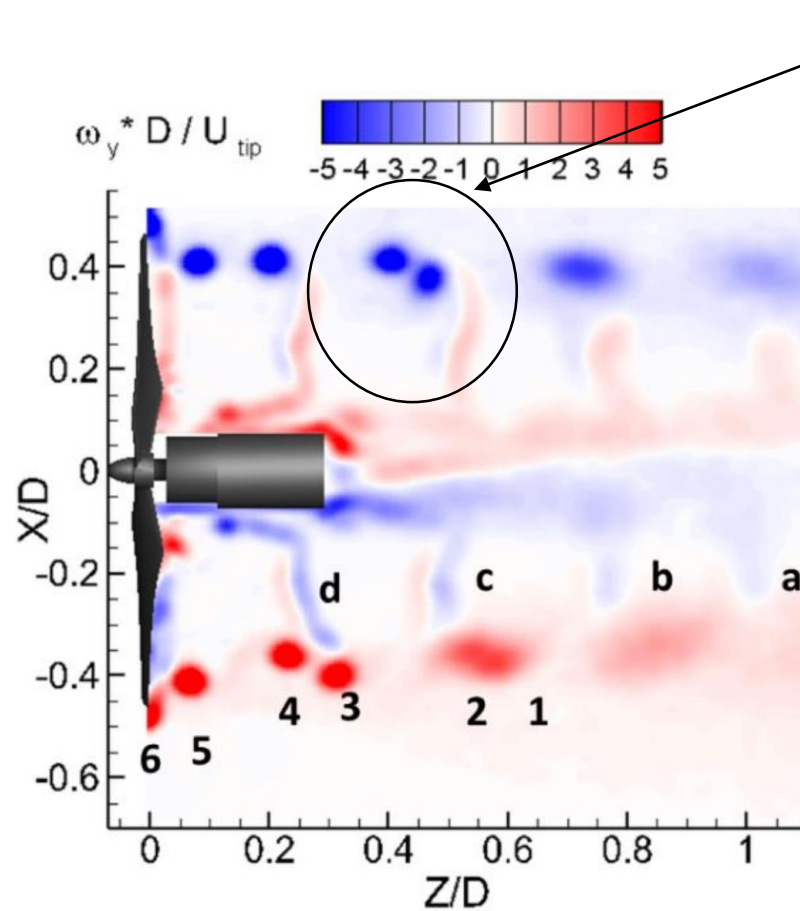
Mean  $C_T$  agreement between 0.5% →

Underpredicted  $C_T$  fluctuations due to not capturing  
hub and mounting-pole interactions →

	Experiment <sup>[1]</sup>	Simulation	Error
Mean $C_T$	0.1007	0.1013	0.5 %
$C_T$ fluctuation	0.008	0.001	

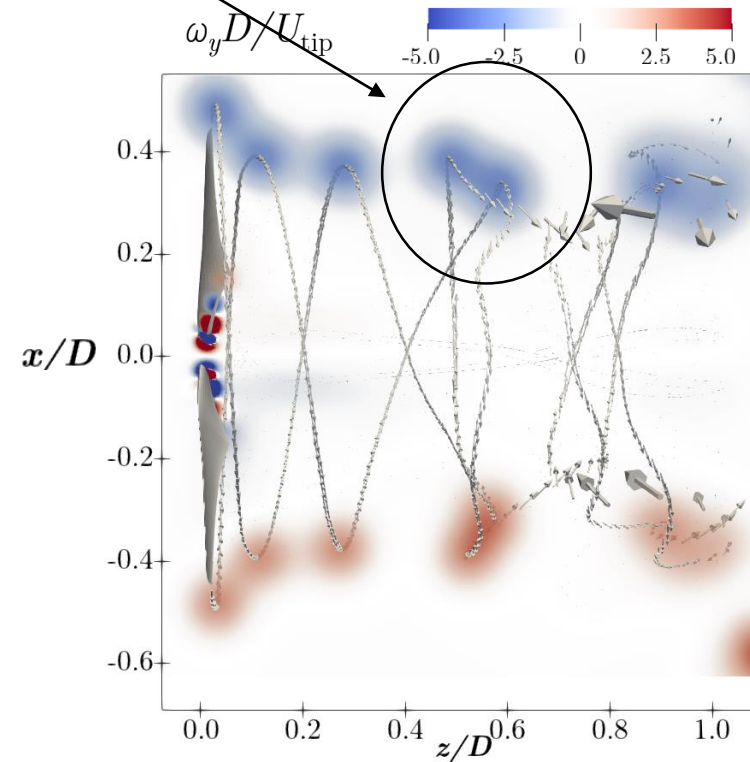
[1] Zhou, W., Ning, Z., Li, H., and Hu, H., 2017, "An Experimental Investigation on Rotor-to-Rotor Interactions of Small UAV Propellers."

# Hover – Individual Rotor



EXPERIMENT<sup>[1]</sup>

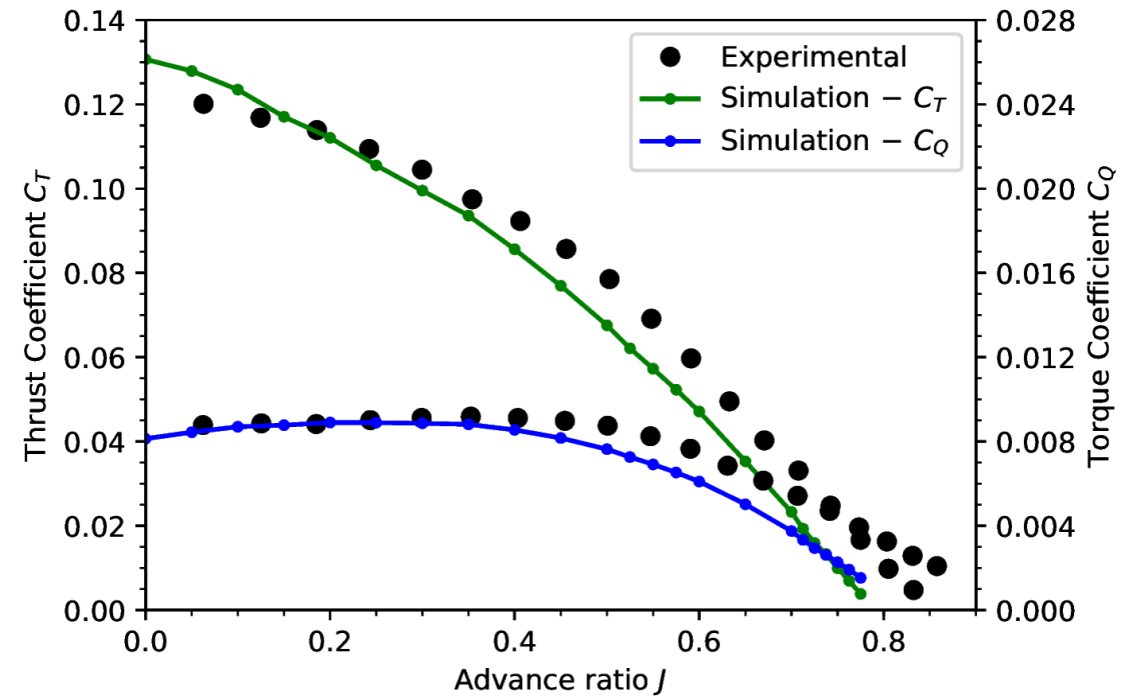
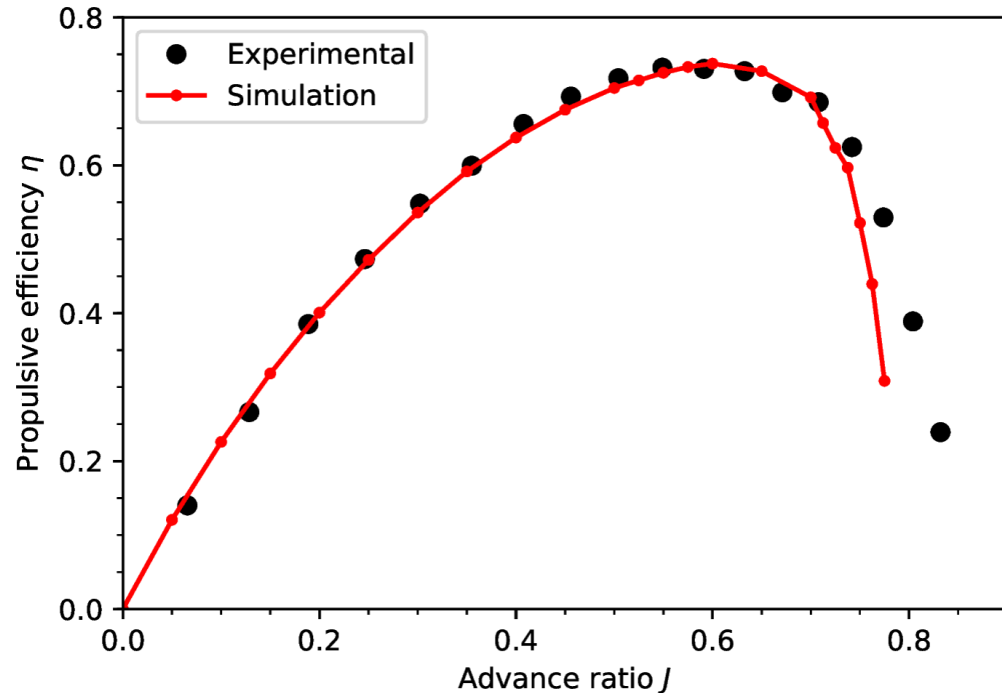
Leapfrogging is accurately predicted at  $z/D \approx 0.5$



SIMULATION

[1] Zhou, W., Ning, Z., Li, H., and Hu, H., 2017, "An Experimental Investigation on Rotor-to-Rotor Interactions of Small UAV Propellers."

# Forward Flight – Individual Rotor



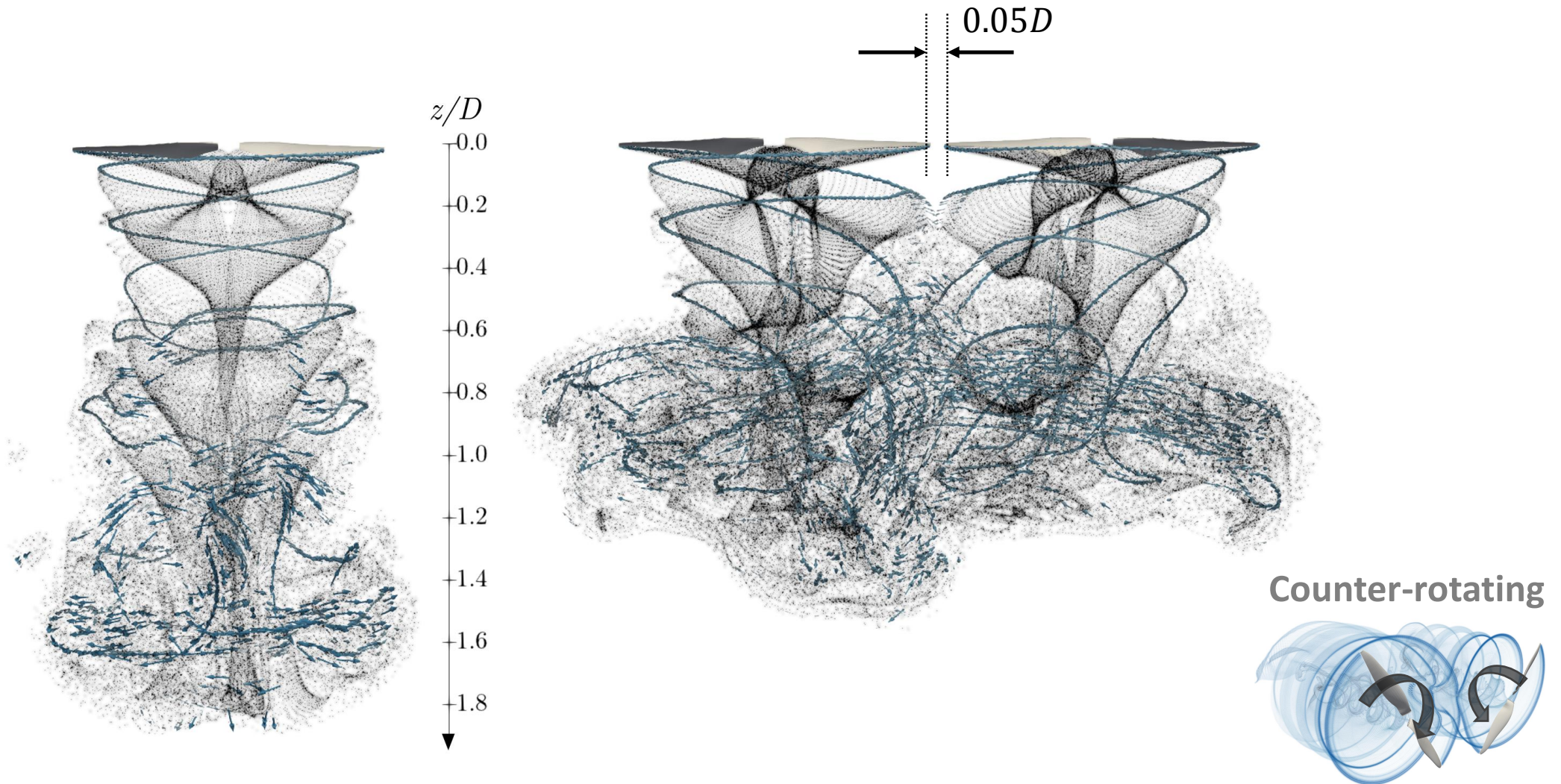
$$\eta = \frac{TU_\infty}{2\pi nQ}$$

$$C_T = \frac{T}{\rho n^2 D^4}$$

$$C_Q = \frac{Q}{\rho n^2 D^5}$$

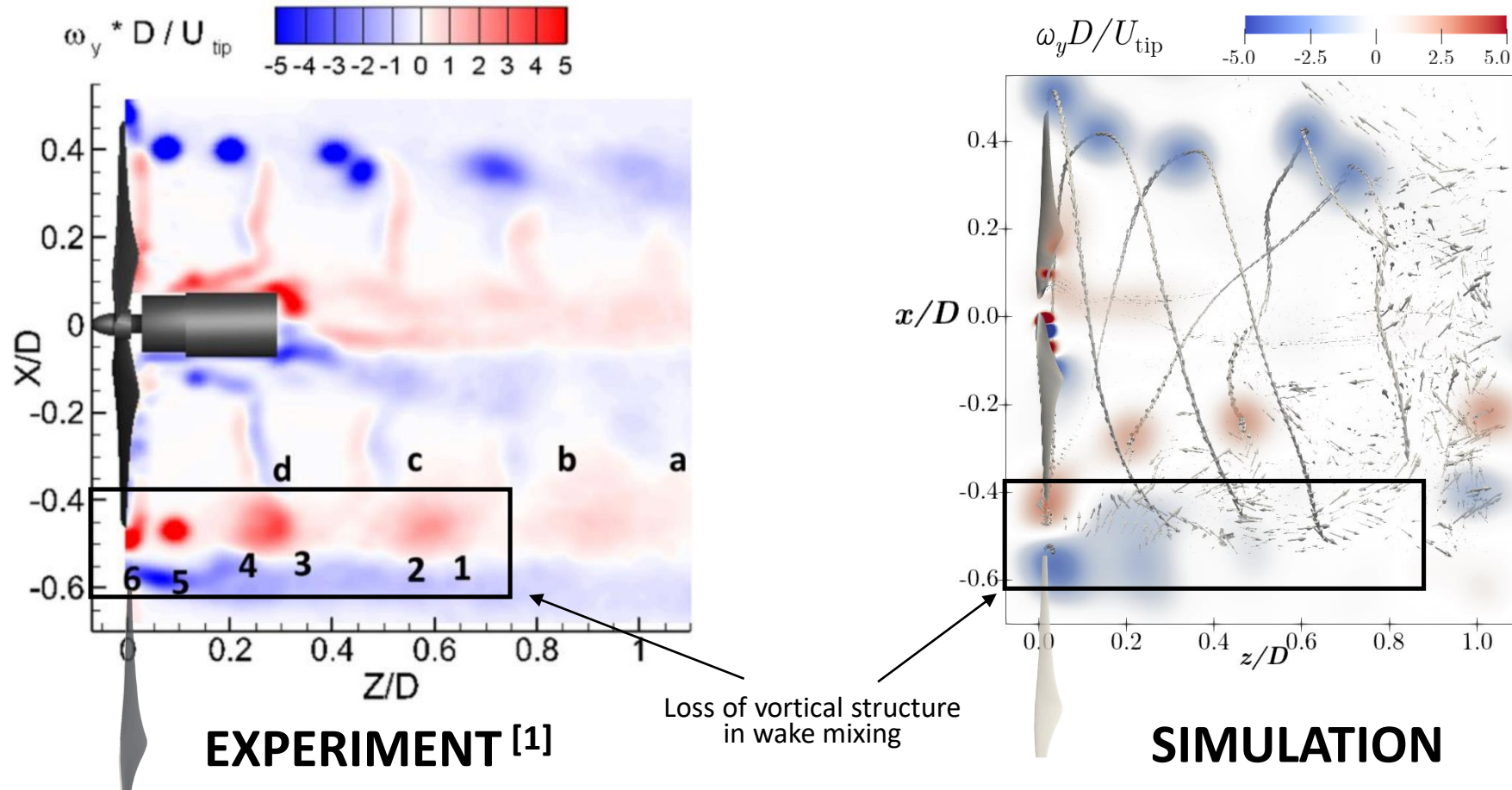
RESULTS  
**MULTIROTOR**

# Hover – Multirotor



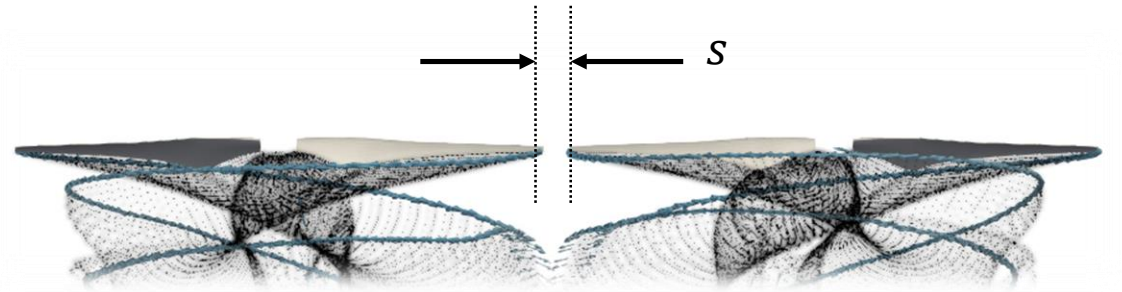


# Hover – Multirotor

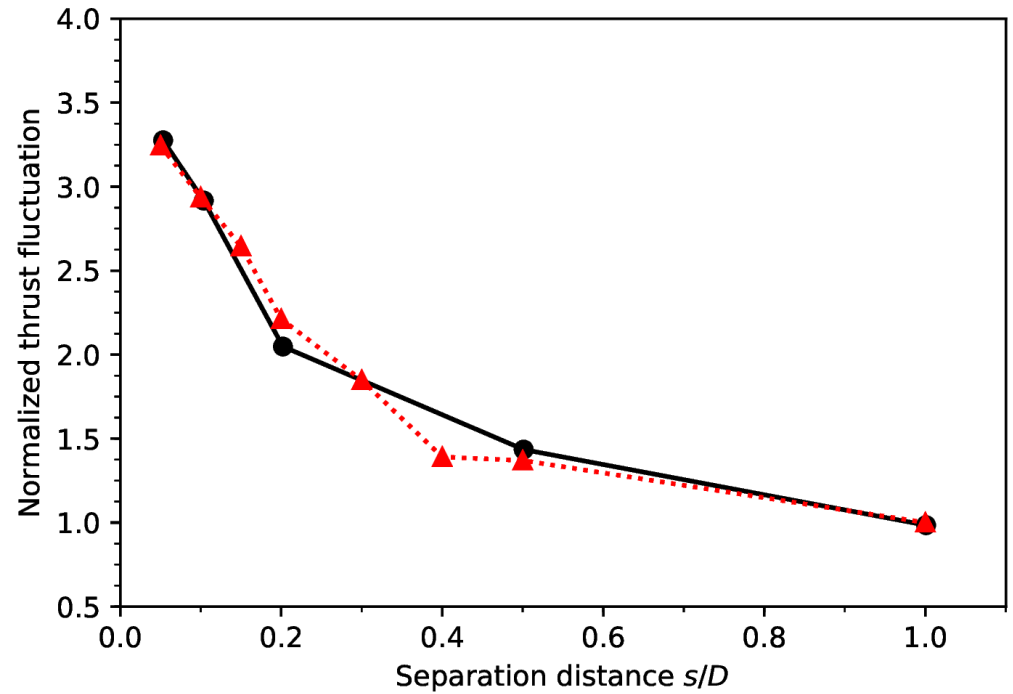
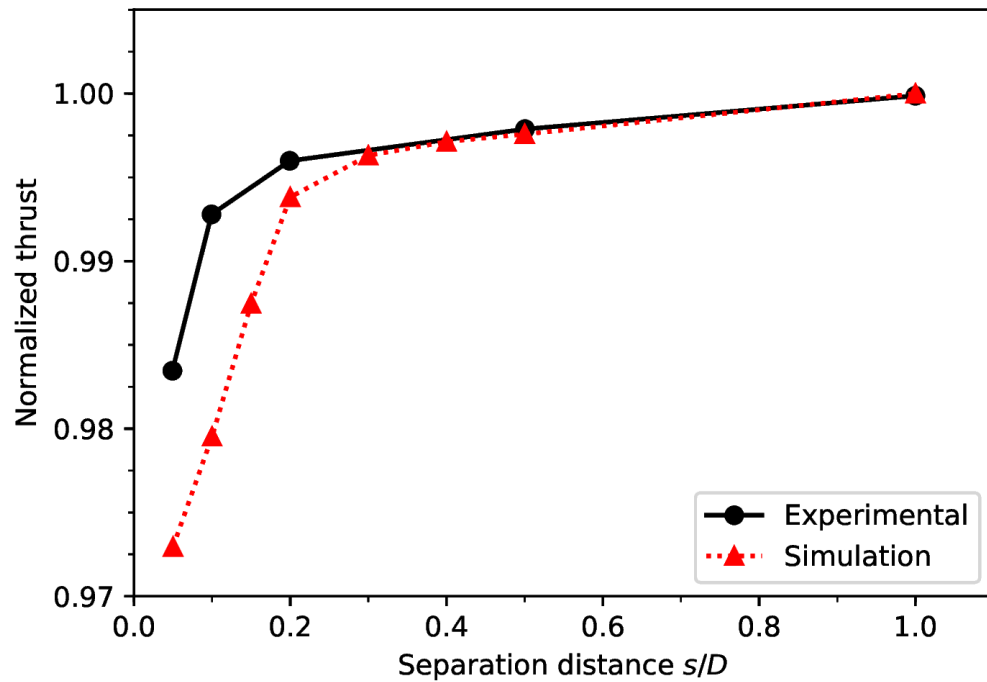




# Hover – Multirotor

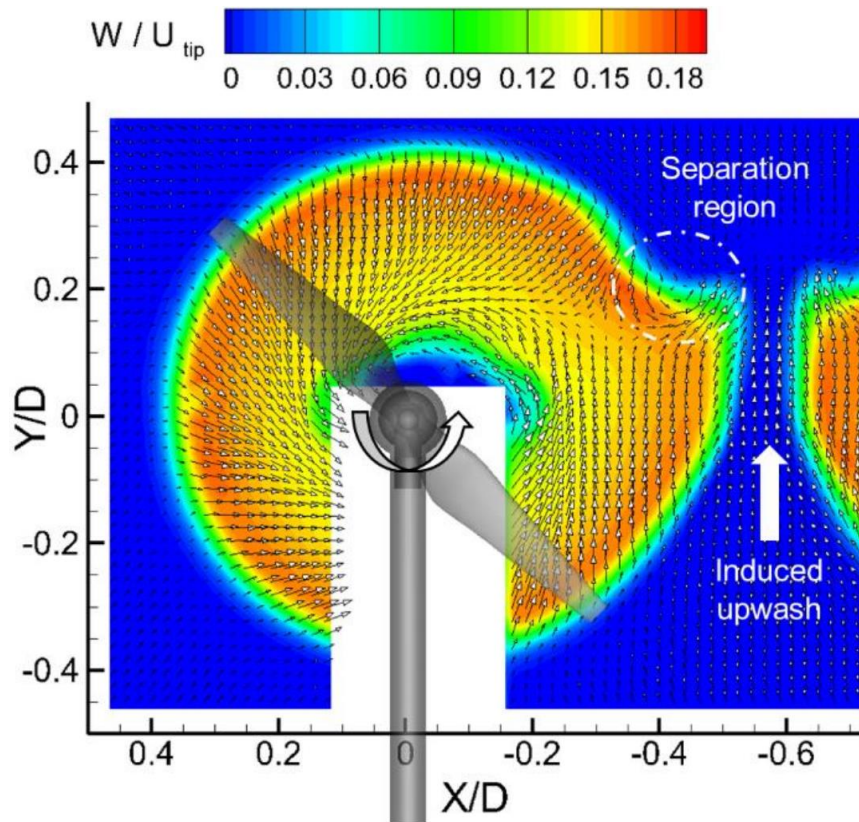


Rotor-on-rotor interactions (thrust drop and unsteady loading) are predicted with sufficient accuracy



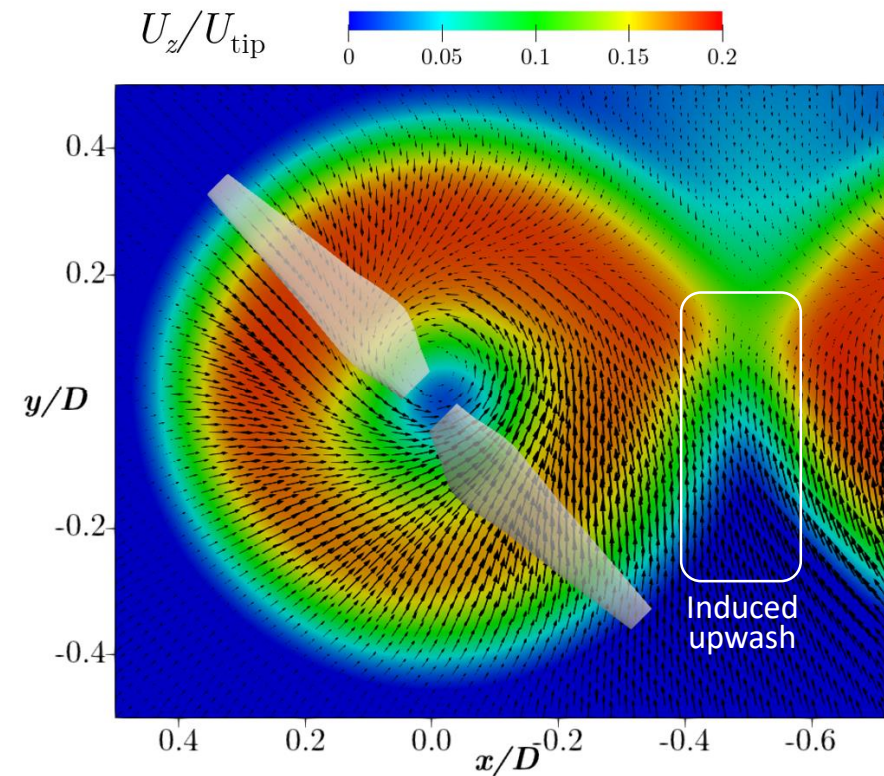
# Hover – Individual Rotor

Simulation captures similar near-field than observed in PIV



EXPERIMENT [1]

## Ensemble Average



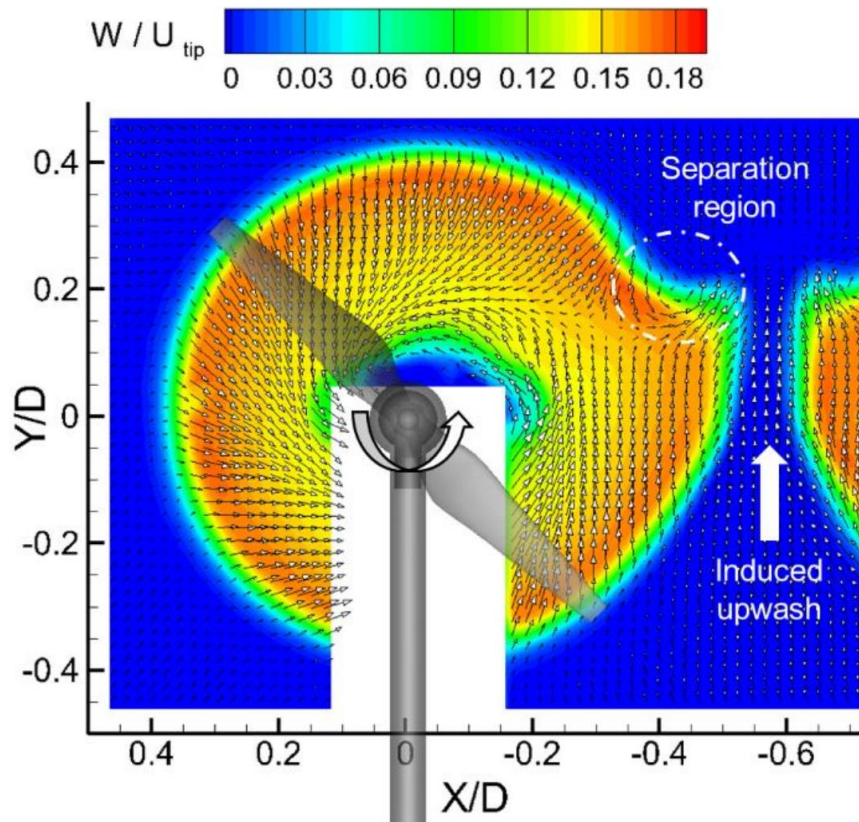
SIMULATION

[1] Zhou, W., Ning, Z., Li, H., and Hu, H., 2017, "An Experimental Investigation on Rotor-to-Rotor Interactions of Small UAV Propellers."



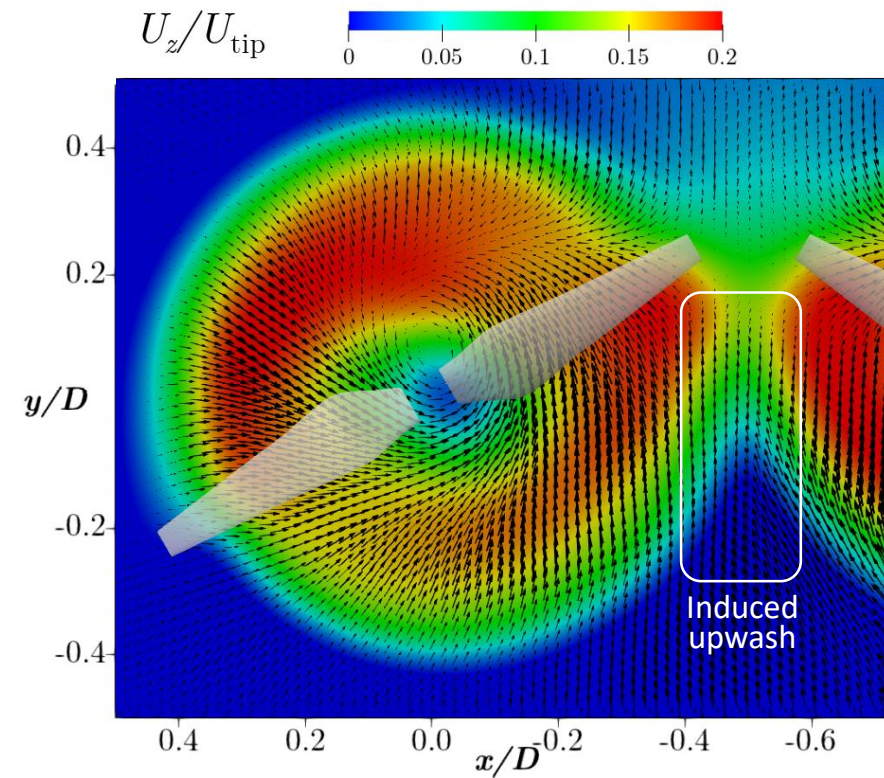
# Hover – Individual Rotor

Simulation captures similar near-field than observed in PIV



**EXPERIMENT [1]**

## Phase-locked



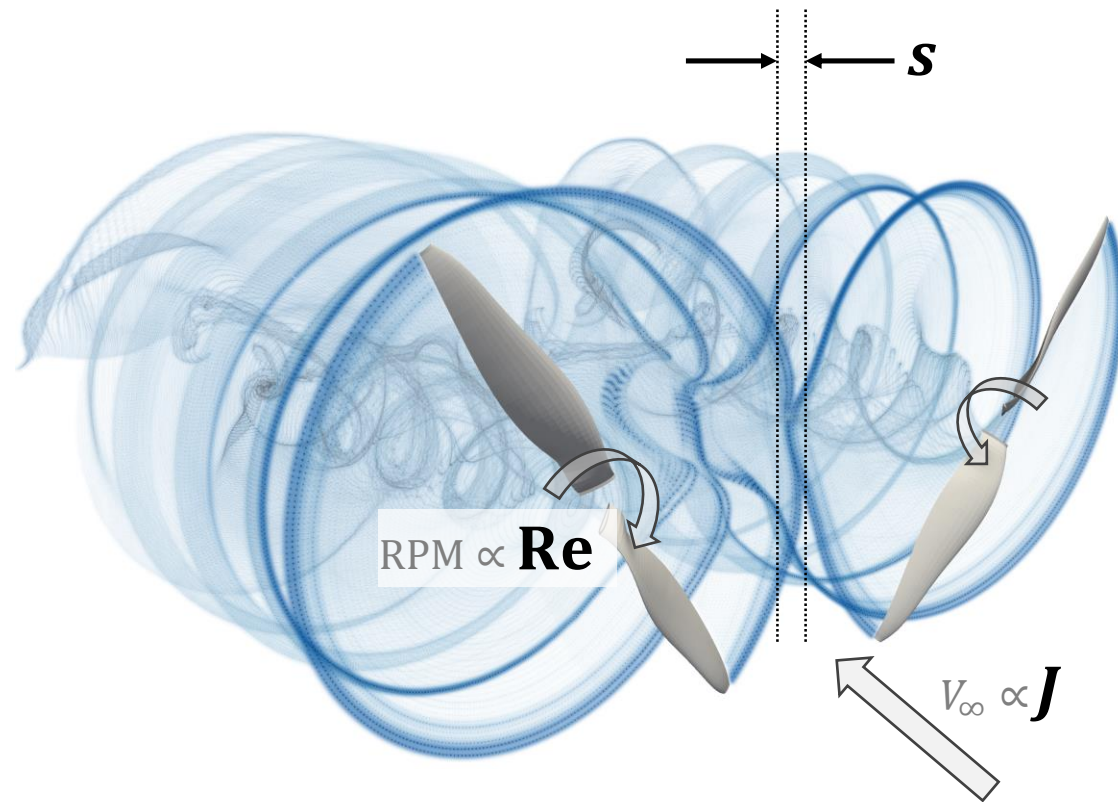
**SIMULATION**

[1] Zhou, W., Ning, Z., Li, H., and Hu, H., 2017, "An Experimental Investigation on Rotor-to-Rotor Interactions of Small UAV Propellers."

RESULTS

# PARAMETRIC STUDY

# Multirotor Parametric Study

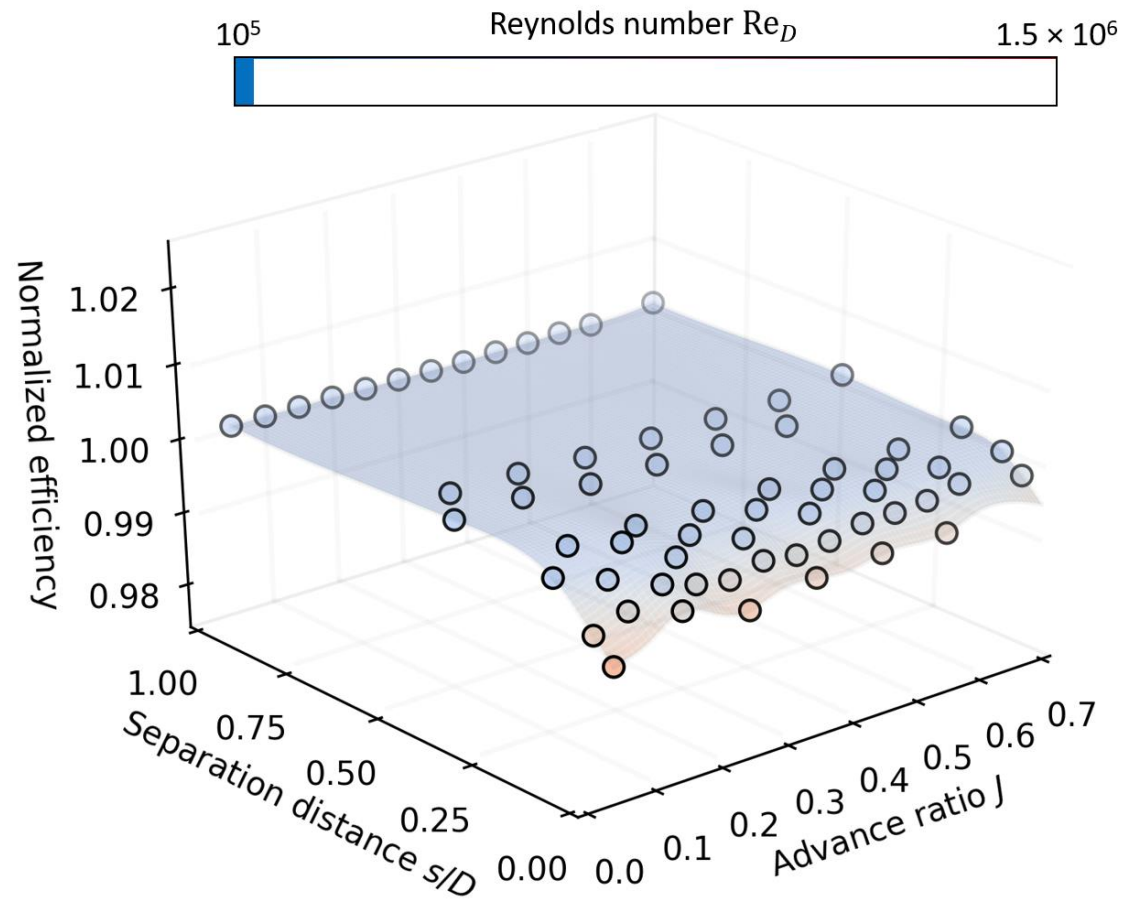


- OPERATIONAL PARAMETERS
  - **Re** – Reynolds number
  - **J** – Advance ratio
  - **s** – Separation
  - Counter or co-rotation
    - ↻ ↻
    - ↻ ↻
- 6 response surfaces
  - $C_T, C_Q, \eta$  – mean and fluctuations
- 1152 simulations
- ~3.5 days on desktop computer
  - Intel(R) Xeon(R) CPU E5-2699 v3 @ 2.30GHz

~4 minutes per simulation

# Multirotor Parametric Study

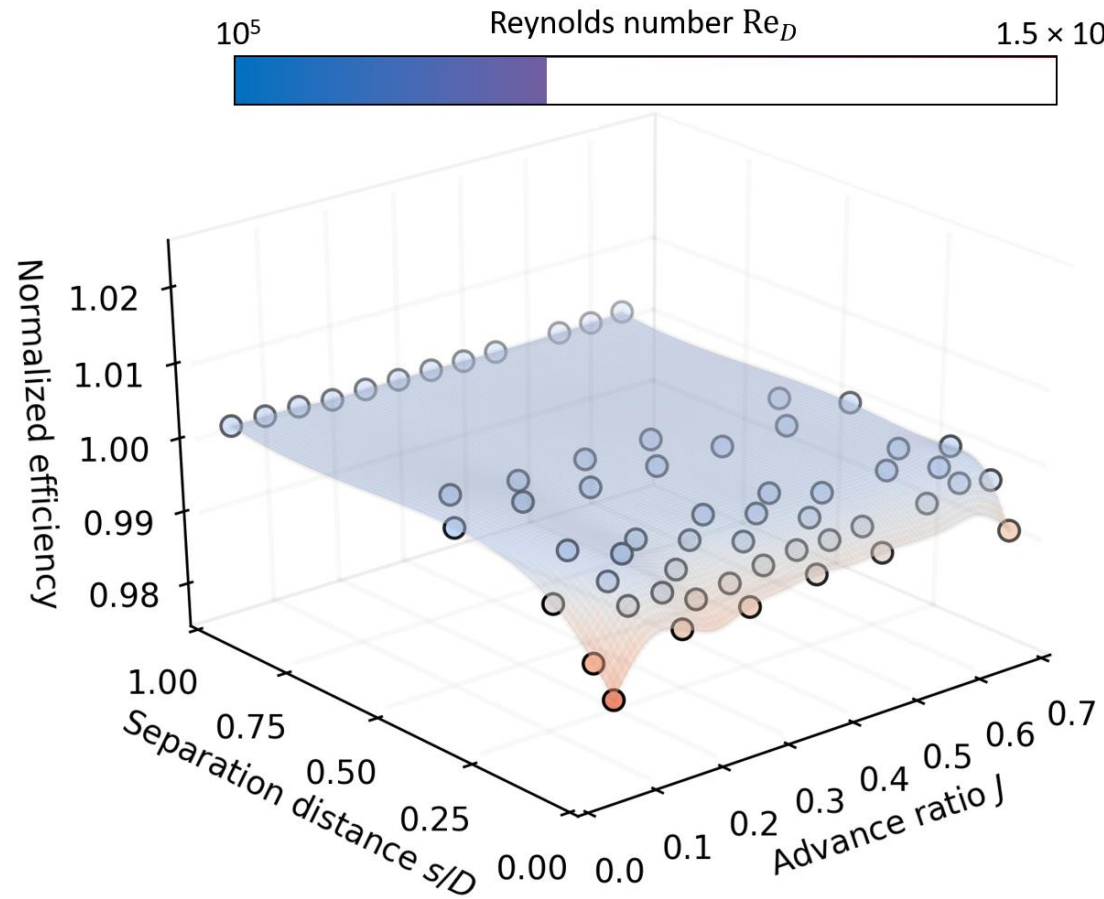
## Efficiency Response Surface



- Performance drops in all configurations
- Largest interactions in hover and near hover
- ~3% max drop

# Multicopter Parametric Study

## Efficiency Response Surface

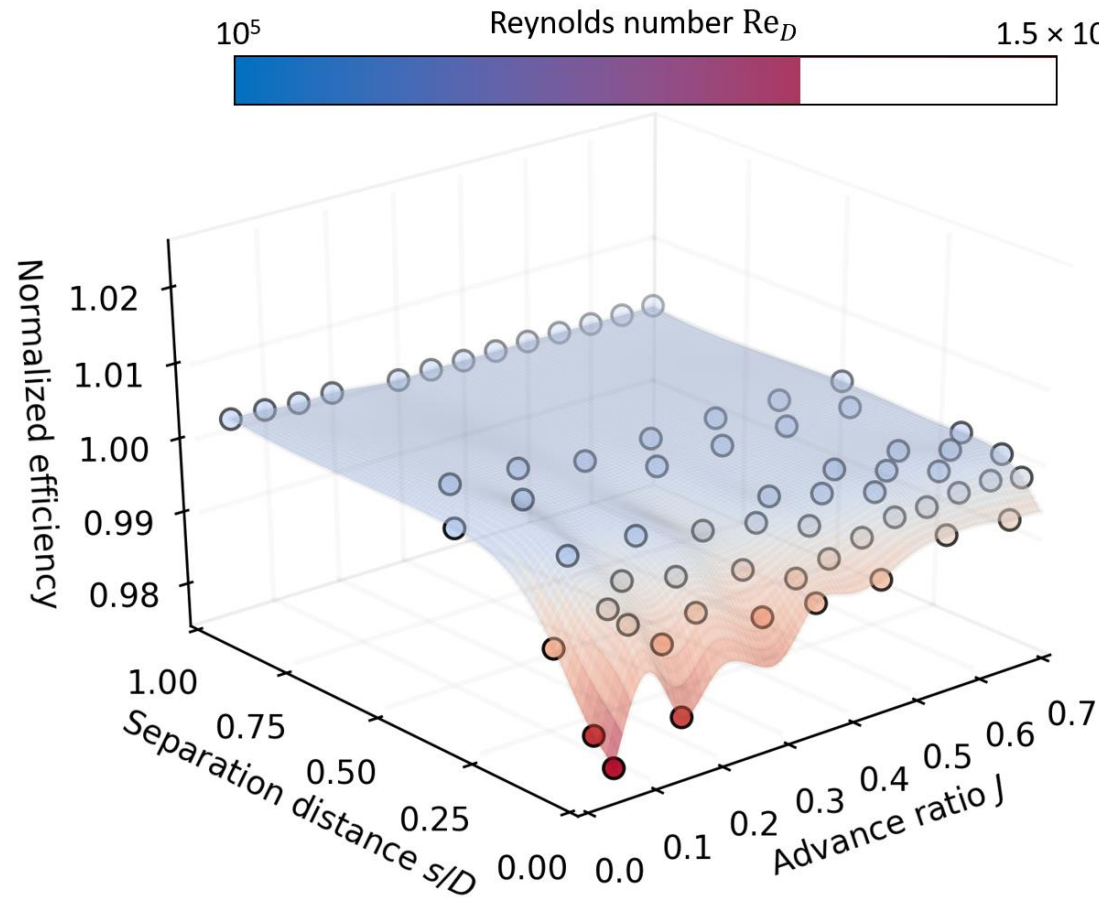


- Performance drops in all configurations
- Largest interactions in hover and near hover
- $\sim 3\%$  max drop



# Multicopter Parametric Study

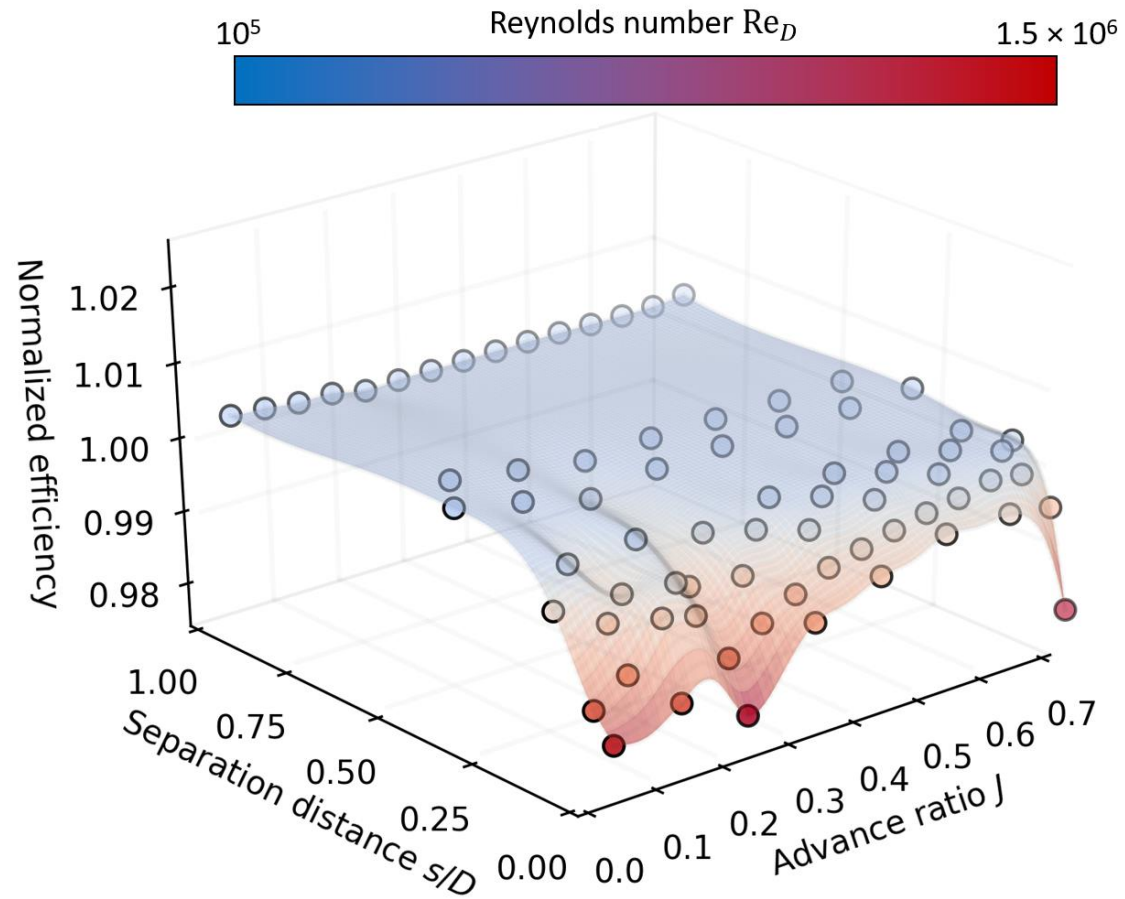
## Efficiency Response Surface



- Performance drops in all configurations
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# Multirotor Parametric Study

## Efficiency Response Surface

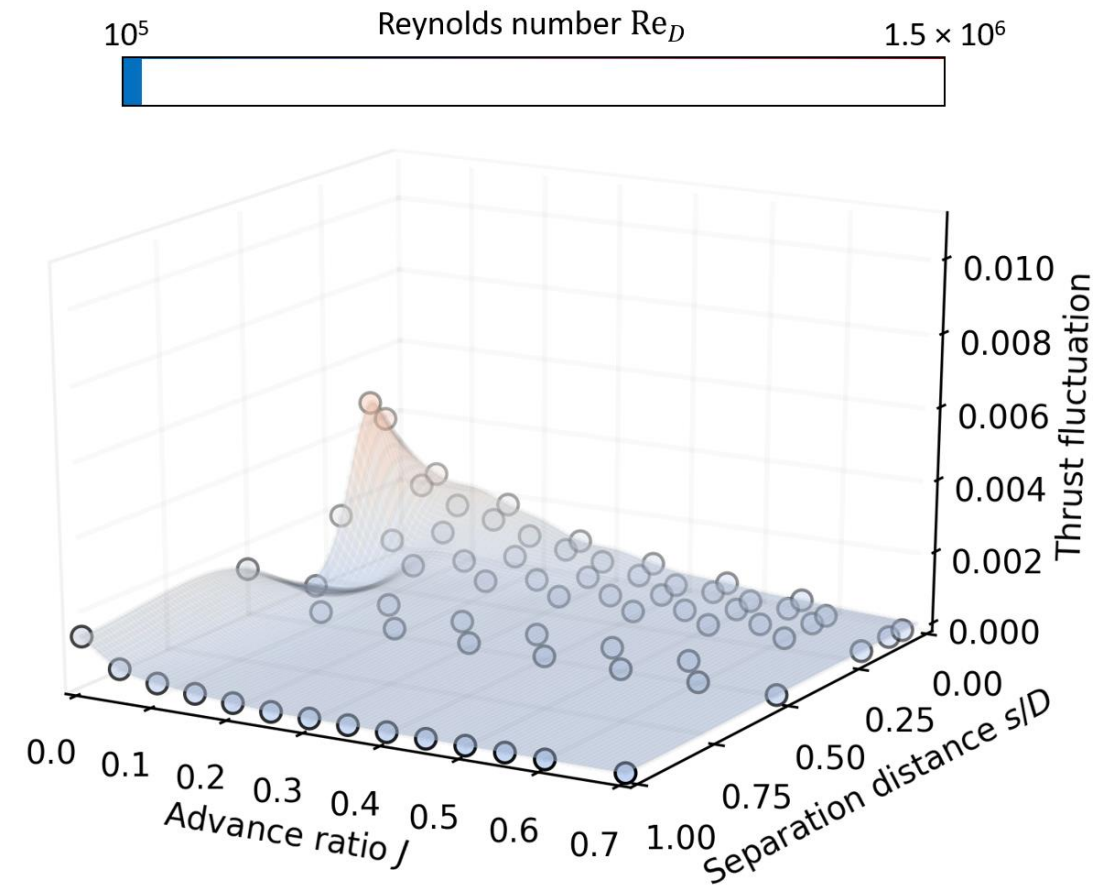


- Performance drops in all configurations
- Largest interactions in hover and near hover
- ~3% max drop

# Multirotor Parametric Study

## Thrust Fluctuation Response Surface

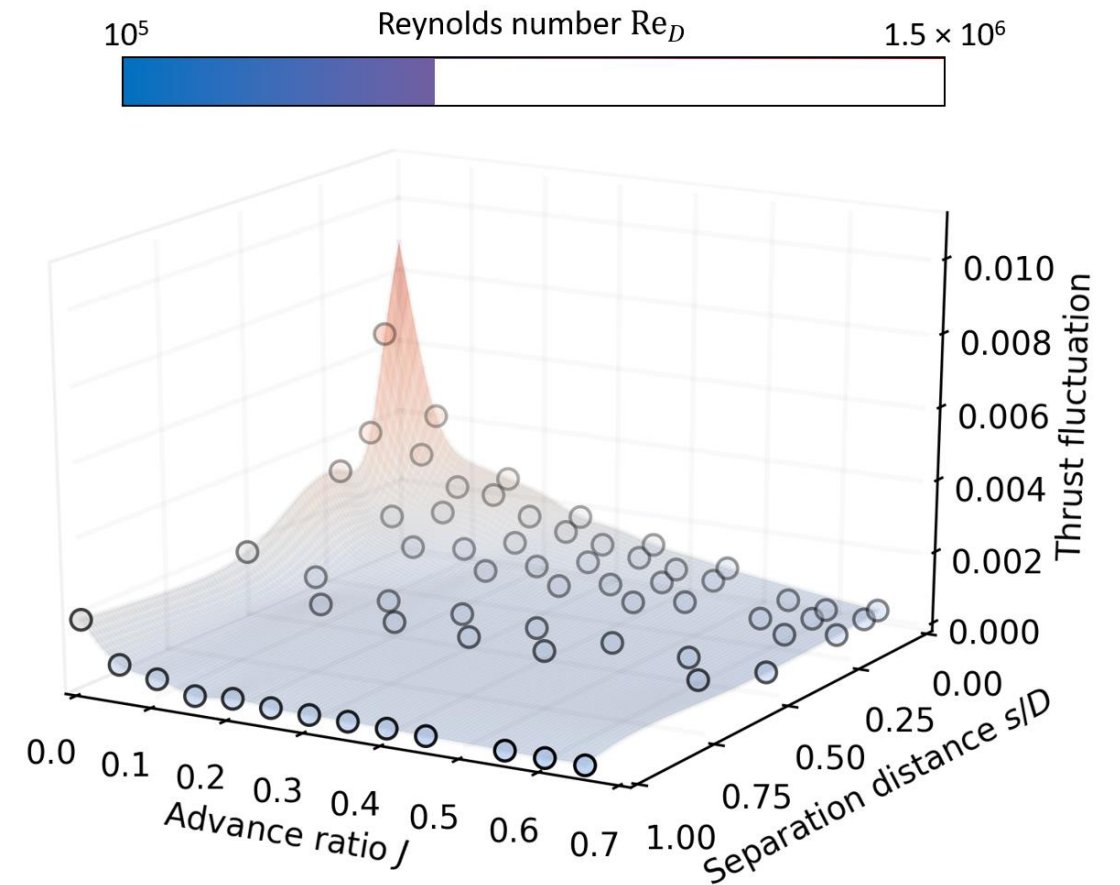
- Largest fluctuations in hover and near-hover
- Fluctuations increase with Reynolds number



# Multicopter Parametric Study

## Thrust Fluctuation Response Surface

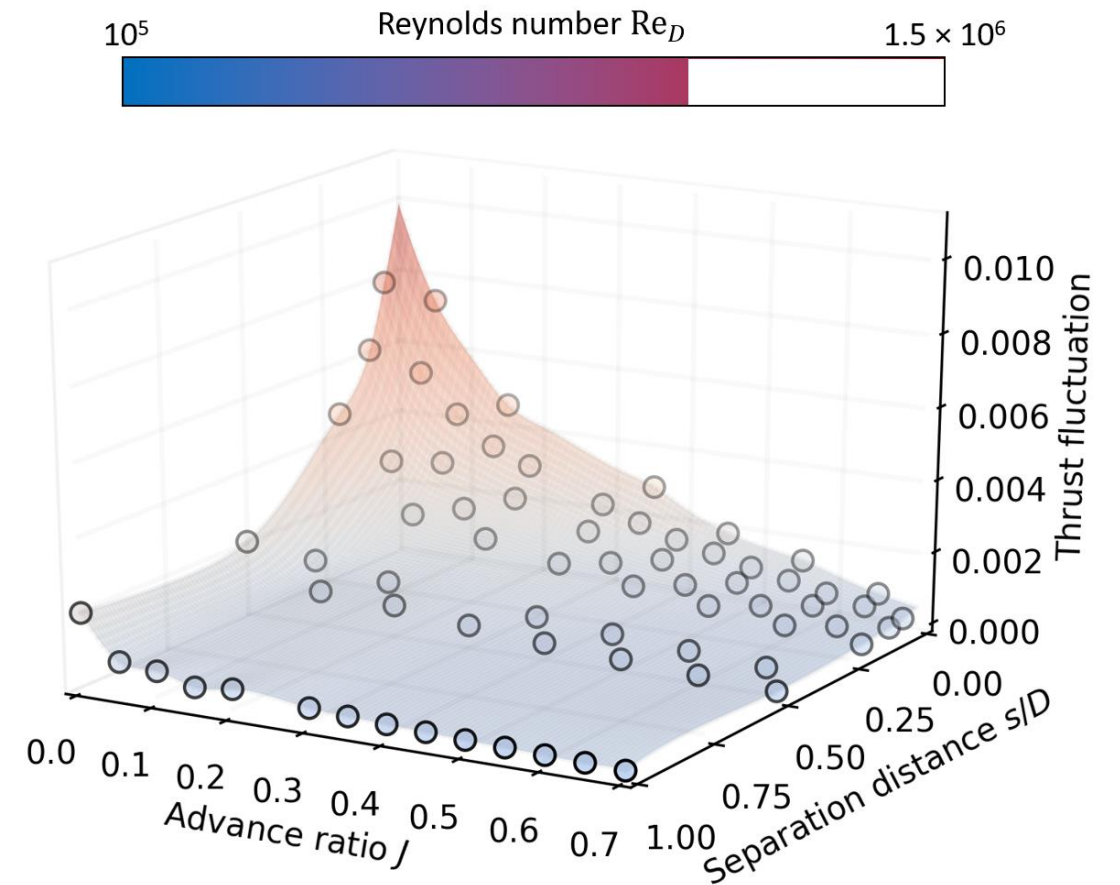
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# Multicopter Parametric Study

## Thrust Fluctuation Response Surface

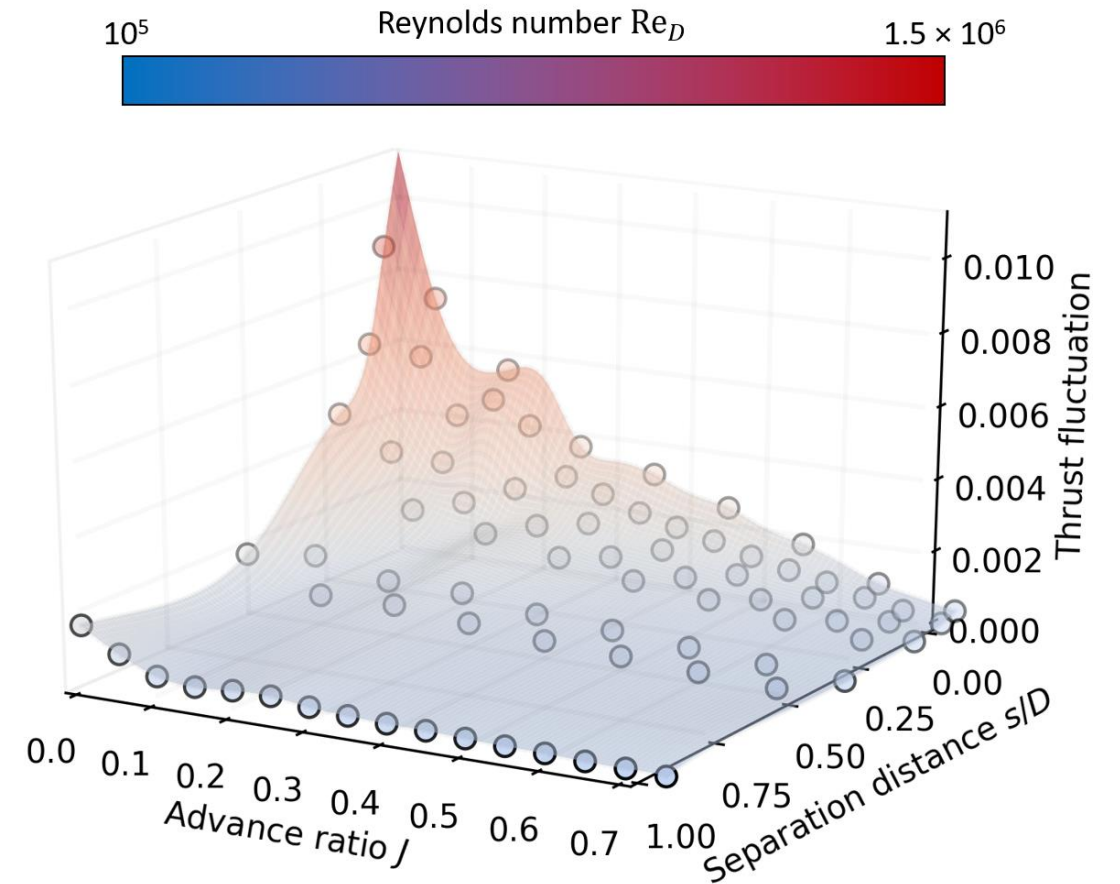
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# Multicopter Parametric Study

## Thrust Fluctuation Response Surface

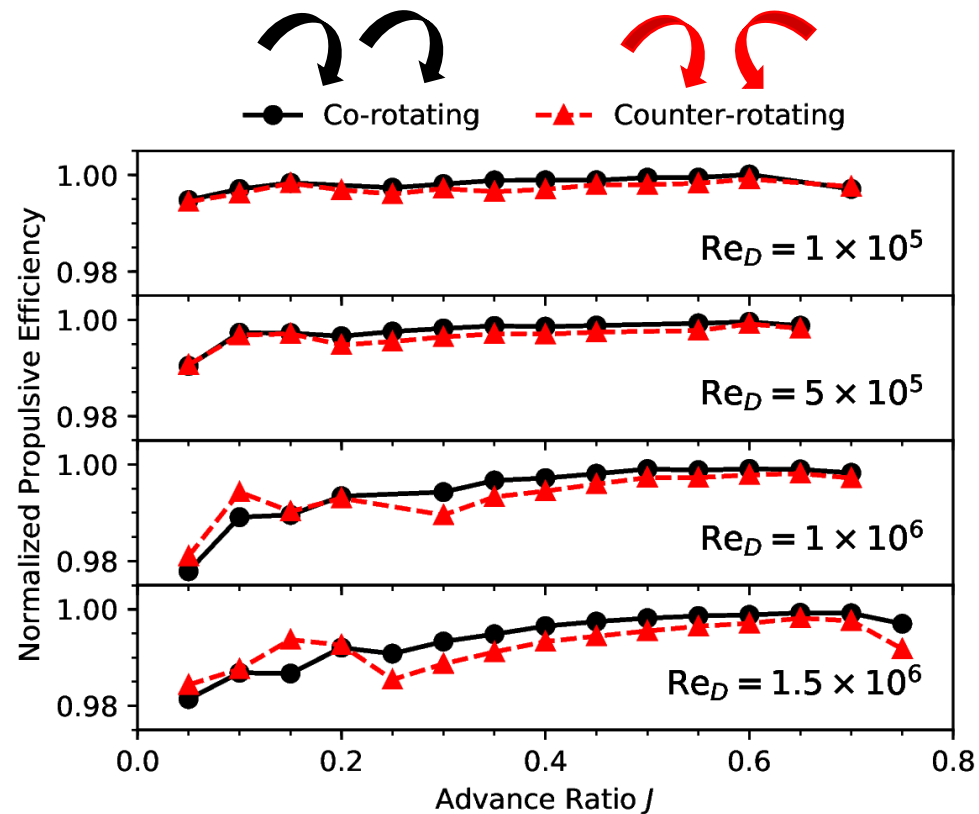
- Largest fluctuations in hover and near-hover
- Fluctuations increase with Reynolds number





# Multirotor Parametric Study

## Co-rotation vs Counter-rotation



- Counter-rotation is slightly less efficient than co-rotation for  $J > 0.25$  (~0.5% less efficient)

# CONCLUSIONS

## VPM multirotor model

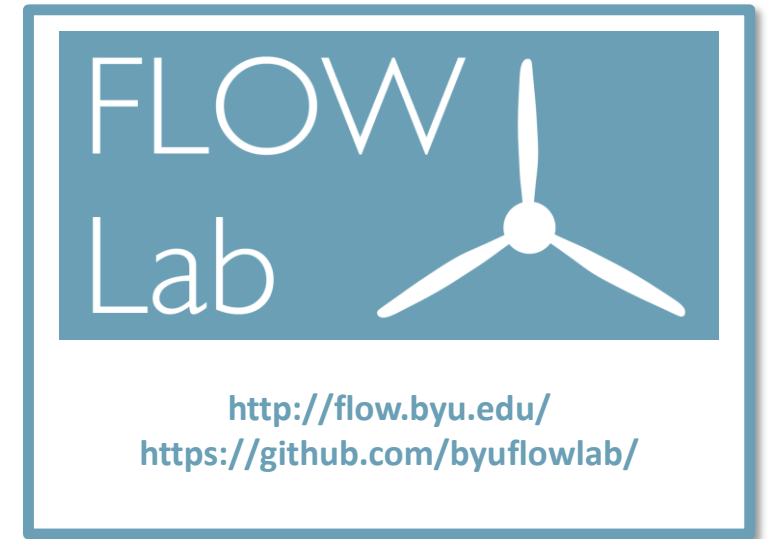
- Validated in hover and forward flight.
- Validated at low and high Reynolds.

## Multirotor parametric study

- Interactions are detrimental across all advance ratios and Reynolds numbers.
- Performance drop accentuated at  $J < 0.2$
- Largest thrust fluctuations at  $J < 0.2$
- Counter-rotation is slightly less efficient at  $J > 0.25$
- Higher Reynolds number accentuates interactions in a lightly tip-loaded rotor.

## FUTURE WORK

- Coupling with FW-H noise code.
- Automatic derivatives for gradient-based design optimization.



Work funded by the High Impact Doctoral Research fellowship granted by BYU

